

# Reducing copies in a Lustre-like language with arrays

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# Table of contents

- 1 Lustre
- 2 Rust
- 3 Reducing copies
- 4 Language and compilation

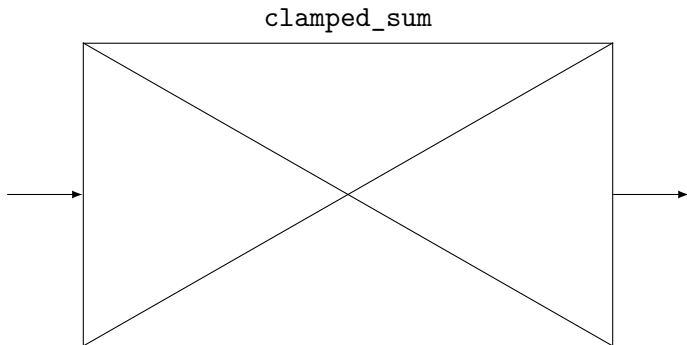
# Table of contents

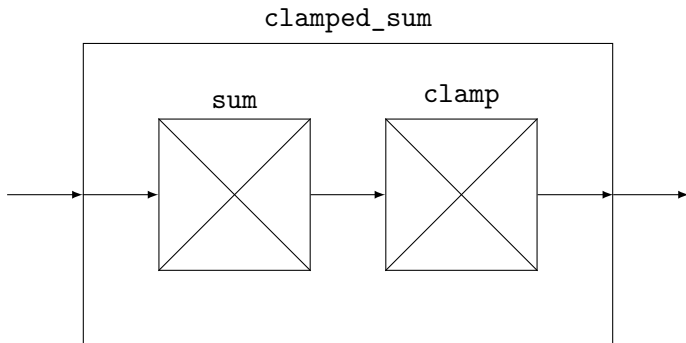
1 Lustre

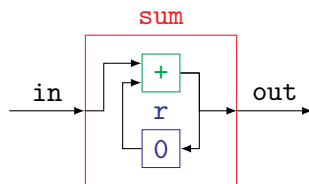
2 Rust

3 Reducing copies

4 Language and compilation



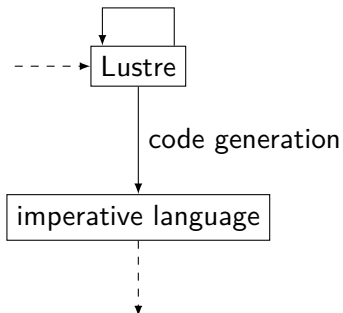




`node sum(in: int) = (out: int)`  $\forall n \in \mathbb{N}, out_n = \sum_{i=0}^n in_i$   
`out = in + last r`  $\forall n \in \mathbb{N}, out_n = in_n + r_{n-1}$   
`r init 0 = out`  $r_{-1} = 0 \wedge \forall n \in \mathbb{N}, r_n = out_n$

# Compilation scheme

static checks then rewriting



# Constraints on code production

- worst case execution time for required responsiveness
- worst case memory consumption for hardware limitations



# Table of contents

1 Lustre

2 Rust

3 Reducing copies

4 Language and compilation

# Ownership

```
fn f(a: T);  
  
fn g(x: T) {  
    let y = x;  
    f(y);  
}
```

# Ownership

```
fn f(a: T);  
  
fn g(x: T) {  
    let y = x;  
    f(x);  
}
```

```
fn f(a: T);  
  
fn g(x: T) {  
    f(x);  
    f(x);  
}
```

# Borrowing

```
fn f(a: &mut T, b: &T, c: &T);
```

```
fn g(x: T, y: &mut T, z: &T) {  
    f(&mut x, ..., ...);  
}
```

# Borrowing

```
fn f(a: &mut T, b: &T, c: &T);
```

```
fn g(x: T, y: &mut T, z: &T) {  
    f(&mut *y, ..., ...);  
}
```

# Borrowing

```
fn f(a: &mut T, b: &T, c: &T);
```

```
fn g(x: T, y: &mut T, z: &T) {  
    f(&mut *z, ..., ...);  
}
```

# Borrowing

```
fn f(a: &mut T, b: &T, c: &T);
```

```
fn g(x: T, y: &mut T, z: &T) {  
    f(..., &x, ...);  
}
```



# Borrowing

```
fn f(a: &mut T, b: &T, c: &T);
```

```
fn g(x: T, y: &mut T, z: &T) {  
    f(..., &*y, ...);  
}
```

# Borrowing

```
fn f(a: &mut T, b: &T, c: &T);
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```
fn g(x: T, y: &mut T, z: &T) {  
    f(..., &*z, ...);  
}
```

# Borrowing

```
fn f(a: &mut T, b: &T, c: &T);
```

```
fn g(x: T, y: &mut T, z: &T) {  
    f(&mut x, &x, ...);  
}
```

# Borrowing

```
fn f(a: &mut T, b: &T, c: &T);
```

```
fn g(x: T, y: &mut T, z: &T) {  
    f(&mut *y, &*y, ...);  
}
```

# Borrowing

```
fn f(a: &mut T, b: &T, c: &T);
```

```
fn g(x: T, y: &mut T, z: &T) {  
    f(&mut x, &*z, &*z);  
}
```

# Borrowing

```
fn f(a: &mut T, b: &T, c: &T);
```

```
fn g(x: T, y: &mut T, z: &T) {  
    f(&mut x, &*y, &*y);  
}
```

# Borrowing

```
fn f(a: &mut T, b: &T, c: &T);
```

```
fn g(x: T, y: &mut T, z: &T) {  
    f(&mut *y, &x, &x);  
}
```

# Safe Rust and Unsafe Rust

- Safe Rust statically ensures the absence of Undefined Behaviors but can't:
  - dereference raw pointers
  - call `unsafe` functions
  - access fields of `unions`
  - and more...
- Unsafe Rust can, but at the cost of fewer guarantees



# Parametric polymorphism and monomorphization

```
fn choose<T>(b: bool, if_true: T, if_false: T)
  -> T {
  if !b { if_false } else { if_true }
}

... choose(b, 1, 2) ...
```

# Parametric polymorphism and monomorphization

```
fn choose<T>(b: bool, if_true: T, if_false: T)
  -> T {
  if !b { if_false } else { if_true }
}

... choose::<int>(b, 1, 2) ...
```

# Parametric polymorphism and monomorphization

```
fn choose<T>(b: bool, if_true: T, if_false: T)
  -> T {
  if !b { if_false } else { if_true }
}
```

```
fn choose_int(b: bool, if_true: int, if_false: int)
  -> int {
  if !b { if_false } else { if_true }
}
```

```
... choose_int(b, 1, 2) ...
```

```
trait Not {  
    type Output;  
    fn not(self) -> Self::Output;  
}  
  
impl Not for &bool {  
    type Output = bool;  
  
    fn not(self) -> Self::Output {  
        ! *self  
    }  
}
```

# Trait polymorphism

```
fn choose<B: Not<Output = bool>, T>  
  (b: B, if_true: T, if_false: T)  
  -> T {  
  if b.not() { if_false } else { if_true }  
}
```

# Trait polymorphism

```
fn choose<B: Not<Output = bool>, T>  
  (b: B, if_true: T, if_false: T)  
  -> T {  
  if <B as Not>::not(b) { if_false } else { if_true }  
}
```

# Trait polymorphism

```
fn choose<T>  
  (b: impl Not<Output = bool>, if_true: T, if_false: T)  
  -> T {  
  if b.not() { if_false } else { if_true }  
}
```

# Table of contents

1 Lustre

2 Rust

**3 Reducing copies**

4 Language and compilation



# Problem: copies introduced during scheduling

```
node fby_42(x: int) = (y: int)
  i init 0 = ((last i) + 1) % 42
  buf init 0^42 = (last buf)[i] <- x
  y = (last buf)[i]
```

# Problem: copies introduced during scheduling

```
node fby_42(x: int) = (y: int)
  i init 0 = ((last i) + 1) % 42
  buf init 0^42 = (last buf)[i] <- x
  y = (last buf)[i]

struct fby_42_state {
  int i;
  int buf[42];
}
```

# Problem: copies introduced during scheduling

```
node fby_42(x: int) = (y: int)
  i init 0 = ((last i) + 1) % 42
  buf init 0^42 = (last buf)[i] <- x
  y = (last buf)[i]

void fby_42_reset(struct fby_42_state *self) {
  self->i = 0;
  for (int i = 0; i < 42; i++) {
    self->buf[i] = 0;
  }
}
```

## Problem: copies introduced during scheduling

```
node fby_42(x: int) = (y: int)
  i init 0 = ((last i) + 1) % 42
  buf init 0^42 = (last buf)[i] <- x
  y = (last buf)[i]

int fby_42_step(struct fby_42_state *self, int x) {
  int buf_tmp[42]; int y;
  self->i = (self->i + 1) % 42;
  memcpy(self->buf, buf_tmp, 42 * sizeof(int));
  buf_tmp[self->i] = x;
  y = self->buf[self->i];
  memcpy(buf_tmp, self->buf, 42 * sizeof(int));
  return y;
}
```

## Problem: copies introduced during scheduling

```
node fby_42(x: int) = (y: int)
  i init 0 = ((last i) + 1) % 42
  y = (last buf)[i]
  buf init 0^42 = (last buf)[i] <- x

int fby_42_step(struct fby_42_state *self, int x) {
  int y;
  self->i = (self->i + 1) % 42;
  y = self->buf[self->i];
  self->buf[self->i] = x;
  return y;
}
```

# Table of contents

1 Lustre

2 Rust

3 Reducing copies

4 Language and compilation

- idea: as early as possible, in the synchronous language, we want to talk about expression addresses in the produced imperative code, to take them into account during scheduling
- language primitives should be as copy-free as possible, making most copies explicit
- we design a highly annotated synchronous language, which would be an intermediate language in a full project
- erase locations to get semantics, erase values to get imperative code

```
struct State { ... }  
impl State {  
  fn reset(&mut self) { ... }  
  fn step(&mut self, ...) -> ... { ... }  
}
```

```
trait Tensor {  
  type Repr;  
  type Idx;  
  type Scal;  
  fn get(ptr: NonNull<Self::Repr>, idx: Self::Idx)  
    -> NonNull<Self::Scal>;  
}
```



```
impl<T> Tensor for Atom<T> {  
    type Repr = T;  
    type Idx = ();  
    type Scal = T;  
  
    fn get(ptr: NonNull<Self::Repr>, idx: Self::Idx)  
        -> NonNull<Self::Scal> {  
        ptr  
    }  
}
```

```
impl<T: Tensor, const N: usize> Tensor for Array<T, N> {  
    type Repr = [T::Repr; N];  
    type Idx = (usize, T::Idx);  
    type Scal = T::Scal;  
  
    fn get(ptr: NonNull<Self::Repr>, idx: Self::Idx)  
        -> NonNull<Self::Scal> {  
        T::get(ptr.cast:::<T::Repr>().add(idx.0), idx.1)  
    }  
}
```

```
trait View: Copy {  
  type Tensor: Tensor;  
  fn get(self, idx: <Self::Tensor as Tensor>::Idx)  
    -> NonNull<<Self::Tensor as Tensor>::Scal>;  
}
```

```
struct Pointer<T: Tensor>(NonNull<T::Repr>);

impl<T: Tensor> View for Pointer<T> {
  type Tensor = T;

  fn get(self, idx: <Self::Tensor as Tensor>::Idx)
    -> NonNull<<Self::Tensor as Tensor>::Scal> {
    T::get(self.0, idx)
  }
}
```

```
struct Projection<V: View>(V, usize);

impl<T: Tensor, const N: usize,
     V: View<Tensor = Array<T, N>>>
  View for Projection<V> {
  type Tensor = T;

  fn get(self, idx: <Self::Tensor as Tensor>::Idx)
    -> NonNull<<Self::Tensor as Tensor>::Scal> {
    self.0.get((self.1, idx))
  }
}
```

$\text{Projection}(v, i) = v[i < N]$

```
struct CutLeft<V: View, const L: usize>(V);

impl<T: Tensor, const N: usize,
     V: View<Tensor = Array<T, N>>, const L: usize>
View for CutLeft<V, L> {
type Tensor = Array<T, L>;

fn get(self, idx: <Self::Tensor as Tensor>::Idx)
  -> NonNull<<Self::Tensor as Tensor>::Scal> {
    self.0.get(idx)
  }
}

(with L < N)
CutLeft::<_, L>(v) =  $\lambda i < L. v[i < N]$ 
```

```
struct CutRight
  <V: View, const L: usize, const R: usize>(V);

impl<T: Tensor, const N: usize,
     V: View<Tensor = Array<T, N>>,
     const L: usize, const R: usize>
View for CutLeft<V, L, R> {
type Tensor = Array<T, R>;

fn get(self, idx: <Self::Tensor as Tensor>::Idx)
  -> NonNull<<Self::Tensor as Tensor>::Scal> {
  self.0.get((idx.0 + L, idx.1))
}
}
(with L + R = N)
CutRight::<_, L, R>(v) =  $\lambda i < R. v[i + L < N]$ 
```

```
struct Repeat<V: View, const N: usize>(V);

impl<V: View, const N: usize> View for Repeat<V, N> {
    type Tensor = Array<V::Tensor, N>;

    fn get(self, idx: <Self::Tensor as Tensor>::Idx)
        -> NonNull<<Self::Tensor as Tensor>::Scal> {
        self.0.get(idx.1)
    }
}
```

$\text{Repeat}::\langle \_, N \rangle(v) = \lambda i < N. v$



```
struct Single<V: View>(V);

impl<V: View> View for Single<V> {
    type Tensor = Array<V::Tensor, 1>;

    fn get(self, idx: <Self::Tensor as Tensor>::Idx)
        -> NonNull<<Self::Tensor as Tensor>::Scal> {
        self.0.get(idx.1)
    }
}
```

$\text{Single}(v) = \lambda i < 1. v$

```
struct Extract<V: View>(V);

impl<T: Tensor, V: View<Tensor = Array<T, 1>>>
  View for Extract<V> {
  type Tensor = T;

  fn get(self, idx: <Self::Tensor as Tensor>::Idx)
    -> NonNull<<Self::Tensor as Tensor>::Scal> {
    self.0.get((0, idx))
  }
}
```

$\text{Extract}(v) = v[0 < 1]$

```
struct Reverse<V: View>(V);

impl<T: Tensor, const N: usize,
     V: View<Tensor = Array<T, N>>>
  View for Reverse<V> {
    type Tensor = Array<T, N>;

    fn get(self, idx: <Self::Tensor as Tensor>::Idx)
      -> NonNull<<Self::Tensor as Tensor>::Scal> {
      self.0.get((N - 1 - idx.0, idx.1))
    }
  }
}
```

$\text{Reverse}(v) = \lambda i < N. v[N - 1 - i < N]$

```
struct Transpose<V: View>(V);

impl<T: Tensor, const N: usize, const M: usize,
     V: View<Tensor = Array<Array<T, M>, N>>>
  View for Transpose<V> {
  type Tensor = Array<Array<T, N>, M>;

  fn get(self, idx: <Self::Tensor as Tensor>::Idx)
    -> NonNull<<Self::Tensor as Tensor>::Scal> {
    self.0.get((idx.1.0, (idx.0, idx.1.1)))
  }
}
```

$\text{Transpose}(v) = \lambda i < M. \lambda j < N. v[j < N] [i < M]$

```
struct Split<V: View, const L: usize, const C: usize>(V);

impl<T: Tensor, const N: usize,
     V: View<Tensor = Array<T, N>>,
     const L: usize, const C: usize>
View for Split<V, L, C> {
type Tensor = Array<Array<T, C>, L>;

fn get(self, idx: <Self::Tensor as Tensor>::Idx)
    -> NonNull<<Self::Tensor as Tensor>::Scal> {
    self.0.get((idx.0 * C + idx.1.0, idx.1.1))
}
}
(with L × C = N)
Split::<_, L, C>(v) = λi < L. λj < C. v[i × C + j < N]
```

```
struct Window<V: View, const W: usize, const S: usize>(V);

impl<T: Tensor, const N: usize,
     V: View<Tensor = Array<T, N>>,
     const W: usize, const S: usize>
View for Window<V, W, S> {
type Tensor = Array<Array<T, W>, S>;

fn get(self, idx: <Self::Tensor as Tensor>::Idx)
    -> NonNull<<Self::Tensor as Tensor>::Scal> {
    self.0.get((idx.0 + idx.1.0, idx.1.1))
}
}
(with W + S - 1 = N)
Window::<_, W, S>(v) =  $\lambda i < S. \lambda j < W. v[i + j < N]$ 
```

```
struct Sample<V: View, const S: usize, const SS: usize>(V);

impl<T: Tensor, const N: usize,
     V: View<Tensor = Array<T, N>>,
     const S: usize, const SS: usize>
View for Sample<V, S, SS> {
type Tensor = Array<T, SS>;

fn get(self, idx: <Self::Tensor as Tensor>::Idx)
    -> NonNull<<Self::Tensor as Tensor>::Scal> {
    self.0.get((idx.0 * S, idx.1))
}
}
(with S × (SS - 1) + 1 = N)
Sample::<_, S, SS>(v) = λi < SS. v[i × S < N]
```

# Calling conventions

```
node(&l_in: int, x @ l_in, ...) = ...
```

```
fn step(&mut self,  
       l_in: impl View<Tensor = Atom<int>>,  
       ...)  
-> ...;
```



# Calling conventions

```
node(&l_in: int, &l_out: int, x @ l_in) = (y @ l_out, ...)
```

```
fn step(&mut self,  
        l_in: impl View<Tensor = Atom<int>>,  
        l_out: impl View<Tensor = Atom<int>>)  
-> ...;
```

# Calling conventions

```
node(&l_in: int, &l_out: int, x @ l_in) = (y @ l_out)
```

```
fn step(&mut self,  
       l_in: impl View<Tensor = Atom<int>>,  
       l_out: impl View<Tensor = Atom<int>>);
```

# Calling conventions

```
node(&l_in: int, x @ l_in) = (&l_out: int, y @ l_out)
```

```
fn step(&mut self,  
       l_in: impl View<Tensor = Atom<int>>)  
-> impl View<Tensor = Atom<int>>;
```

# Calling conventions

```
node(&l_in: int, &mut l_out: int, x @ l_in) = (y @ l_out)
```

```
fn step(&mut self,  
       l_in: impl View<Tensor = Atom<int>>,  
       l_out: impl View<Tensor = Atom<int>>);
```

# Calling conventions

```
node(&mut l_in: int, &mut l_out: int, x @ l_in) =  
    (y @ l_out)
```

```
fn step(&mut self,  
        l_in: impl View<Tensor = Atom<int>>,  
        l_out: impl View<Tensor = Atom<int>>);
```

# Memories

```
memories (fby_0_n init 0: int @ l_mem)

struct State {
  l_mem: MaybeUninit<<Atom<int> as Tensor>::Repr>,
  ...
}

fn reset(&mut self) { self.l_mem.write(0); ... }

fn step(&mut self, ...) {
  let l_mem: Pointer<Atom<int>> =
    Pointer(
      NonNull::new_unchecked(
        self.l_mem.as_mut_ptr()));
  ...
}
```

```
stack (&mut l_loc: int)

fn step(&mut self, ...) {
    let l_loc: Pointer<Atom<int>> =
        Pointer(
            NonNull::new_unchecked(
                MaybeUninit::uninit().as_mut_ptr()));
    ...
}
```

# Variables locales

```
locals (a @ l_in) (b @ l_out) (c @ l_mem) (d @ l_loc)
```



# Clocks and views

```
node ex(c: bool, in) = (out)
  tmp = f(in when c)
  out = g(merge(c, tmp, in when not c))
```

c	T	F	T	T	F	...
in	<i>in</i> <sub>0</sub>	<i>in</i> <sub>1</sub>	<i>in</i> <sub>2</sub>	<i>in</i> <sub>3</sub>	<i>in</i> <sub>4</sub>	...
in when c	<i>in</i> <sub>0</sub>		<i>in</i> <sub>2</sub>	<i>in</i> <sub>3</sub>		...
tmp	<i>tmp</i> <sub>0</sub>		<i>tmp</i> <sub>2</sub>	<i>tmp</i> <sub>3</sub>		...
in when not c		<i>in</i> <sub>1</sub>			<i>in</i> <sub>4</sub>	...
merge(c, tmp, in when not c)	<i>tmp</i> <sub>0</sub>	<i>in</i> <sub>1</sub>	<i>tmp</i> <sub>2</sub>	<i>tmp</i> <sub>3</sub>	<i>in</i> <sub>4</sub>	...
out	<i>out</i> <sub>0</sub>	<i>out</i> <sub>1</sub>	<i>out</i> <sub>2</sub>	<i>out</i> <sub>3</sub>	<i>out</i> <sub>4</sub>	...

# Clocks and views

```
node ex(c: bool, in) = (out)
  tmp = f(in when c)
  out = g(merge(c, tmp, in when not c))
```

c	T	F	T	T	F	...
in	<i>in</i> <sub>0</sub>	<i>in</i> <sub>1</sub>	<i>in</i> <sub>2</sub>	<i>in</i> <sub>3</sub>	<i>in</i> <sub>4</sub>	...
in when c	<i>in</i> <sub>0</sub>	?	<i>in</i> <sub>2</sub>	<i>in</i> <sub>3</sub>	?	...
tmp	<i>tmp</i> <sub>0</sub>	?	<i>tmp</i> <sub>2</sub>	<i>tmp</i> <sub>3</sub>	?	...
in when not c	?	<i>in</i> <sub>1</sub>	?	?	<i>in</i> <sub>4</sub>	...
merge(c, tmp, in when not c)	<i>tmp</i> <sub>0</sub>	<i>in</i> <sub>1</sub>	<i>tmp</i> <sub>2</sub>	<i>tmp</i> <sub>3</sub>	<i>in</i> <sub>4</sub>	...
out	<i>out</i> <sub>0</sub>	<i>out</i> <sub>1</sub>	<i>out</i> <sub>2</sub>	<i>out</i> <sub>3</sub>	<i>out</i> <sub>4</sub>	...

$$\frac{c: C_1 + \dots + C_n \quad x @ l}{x \text{ when } c = C_i @ l \text{ on } c = C_i}$$

$$\frac{c: C_1 + \dots + C_n \quad \forall i, e_i @ l \text{ on } c = C_i}{\text{merge}(c, C_1 \Rightarrow e_1, \dots, C_n \Rightarrow e_n) @ l}$$

# Arrays and views

$$\frac{l: [T; M + N] \quad x @ l}{\text{fst}(x \text{ as } [_; M] ++ [_; N]) @ \text{fst}(l \text{ as } [_; M] ++ [_; N])}$$
$$\frac{l: [T; M + N] \quad x @ l}{\text{snd}(x \text{ as } [_; M] ++ [_; N]) @ \text{snd}(l \text{ as } [_; M] ++ [_; N])}$$
$$\frac{x @ \text{fst}(l \text{ as } [_; M] ++ [_; N]) \\ y @ \text{snd}(l \text{ as } [_; M] ++ [_; N])}{x ++ y @ l}$$

# Arrays and views

$$\begin{array}{l} l: [T; N] \quad x @ l \\ \hline x[i] @ l[i] \end{array}$$

# Arrays and views

$$\frac{l: [T; N] \quad x @ l}{x[i] @ l[i]}$$

$$\frac{l: [T; N] \quad x @ l}{x[\backslash i] @ l[\backslash i]}$$

$$\frac{x @ l[i] \quad y @ l[\backslash i]}{\text{update}(y, x) @ l}$$

`[arr with i <- x] = update(arr[\i], x)`

# Arrays and views

$$\frac{x @ 1}{[x] * N @ [1] * N}$$

# Interference of views

$$\frac{l_1 \neq l_2}{l_1 \parallel l_2}$$

$$\frac{i \neq j}{v \text{ on } c = C_i \parallel v \text{ on } c = C_j}$$

$$\frac{}{\text{fst}(v \text{ as } [_; M] ++ [_; N]) \parallel \text{snd}(v \text{ as } [_; M] ++ [_; N])}$$

$$\frac{}{v[i] \parallel v[\backslash i]}$$

$$\frac{v_1 \parallel v_2}{v_2 \parallel v_1}$$

$$\frac{v_1 \parallel v_2}{v_1 \text{ on } c = C \parallel v_2}$$

$$\frac{v_1 \parallel v_2}{[v_1] * N \parallel v_2}$$

...



# Node call and reset

```
b = (f on c1 = C1 reset every c2 = C2, c3 = C3)
    (N; idx, e_idx; &l, a, &mut l' on a = true)
```

$$\forall s, \forall i_1 i_2,$$
$$\forall (\&l_1: \text{bool})(x @ l_1)(\&mut l_2: [\text{int}; s] \text{ on } x = \text{true}),$$
$$\exists (y @ l_2[i_1])$$

```
struct State {
    instance_f_42: State_f<N>,
    ...
}
if let C1 = l_c1.get(()).read() {
    self.instance_f_42
        .step(idx, l_e_idx.get(()).read() as usize, l, l');
}
```

# Node call and reset

```
b = (f on c1 = C1 reset every c2 = C2, c3 = C3)
    (N; idx, e_idx; &l, a, &mut l' on a = true)
```

$$\forall s, \forall i_1 i_2,$$
$$\forall (\&l_1: \text{bool})(x @ l_1)(\&mut l_2: [\text{int}; s] \text{ on } x = \text{true}),$$
$$\exists (y @ l_2[i_1])$$

```
struct State {
    instance_f_42: State_f<N>,
    ...
}
if let C2 = l_c2.get(()).read() {
    self.instance_f_42.reset();
}
```

# Node call and reset

```
b = (f on c1 = C1 reset every c2 = C2, c3 = C3)
    (N; idx, e_idx; &l, a, &mut l' on a = true)
```

$$\forall s, \forall i_1 i_2,$$
$$\forall (\&l_1: \text{bool})(x @ l_1)(\&mut l_2: [\text{int}; s] \text{ on } x = \text{true}),$$
$$\exists (y @ l_2[i_1])$$

```
struct State {
    instance_f_42: State_f<N>,
    ...
}
if let C3 = l_c3.get(()).read() {
    self.instance_f_42.reset();
}
```

# Node call and reset

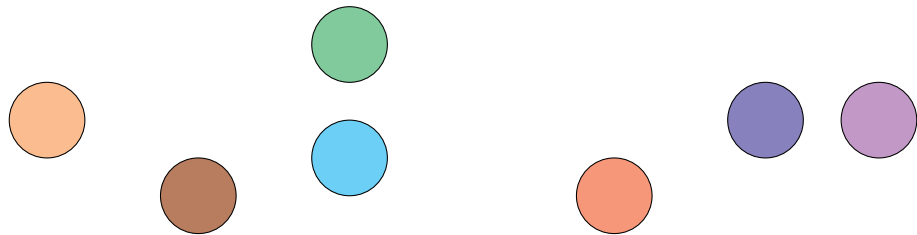
```
b = (f on c1 = C1 reset every c2 = C2, c3 = C3)
    (N; idx, e_idx; &l, a, &mut l' on a = true)
```

$$\forall s, \forall i_1 i_2,$$
$$\forall (\&l_1: \text{bool})(x @ l_1)(\&mut l_2: [\text{int}; s] \text{ on } x = \text{true}),$$
$$\exists (y @ l_2[i_1])$$

```
struct State {
    instance_f_42: State_f_N,
    ...
}
if let C3 = l_c3.get(()).read() {
    self.instance_f_42.reset();
}
```

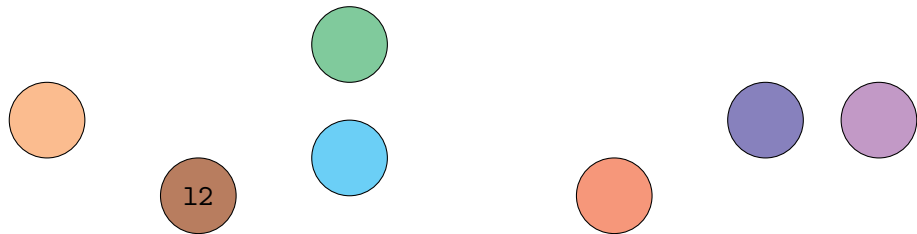
# Scheduling

```
node(&mut l1: int, x @ l1) = (z @ l1)
  stack (&mut l2: bool)
  locals (c1 @ l2) (c2 @ l2) (y @ l1 on c1)
  c1 = i(&mut l2)
  c2 = h(&mut l2)
  y = (f on c1)(&mut l1 on c1, x when c1)
  z = (g reset every c1)
    (&l2, &mut l1, c2, merge(c1, y, x whenot c1))
```



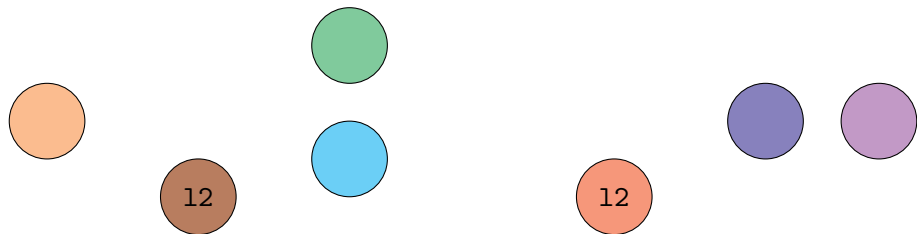
# Scheduling

```
node(&mut l1: int, x @ l1) = (z @ l1)
  stack (&mut l2: bool)
  locals (c1 @ l2) (c2 @ l2) (y @ l1 on c1)
  c1 = i(&mut l2)
  c2 = h(&mut l2)
  y = (f on c1)(&mut l1 on c1, x when c1)
  z = (g reset every c1)
      (&l2, &mut l1, c2, merge(c1, y, x whenot c1))
```



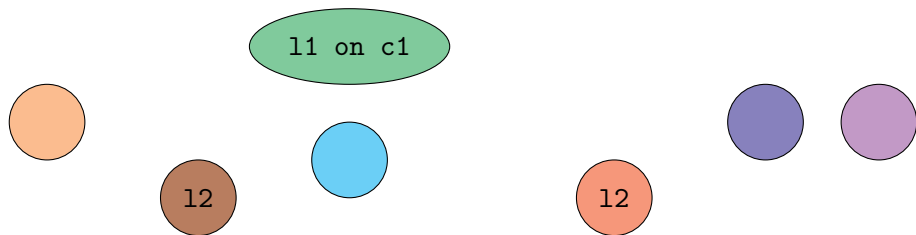
# Scheduling

```
node(&mut l1: int, x @ l1) = (z @ l1)
  stack (&mut l2: bool)
  locals (c1 @ l2) (c2 @ l2) (y @ l1 on c1)
  c1 = i(&mut l2)
  c2 = h(&mut l2)
  y = (f on c1)(&mut l1 on c1, x when c1)
  z = (g reset every c1)
      (&l2, &mut l1, c2, merge(c1, y, x whenot c1))
```



# Scheduling

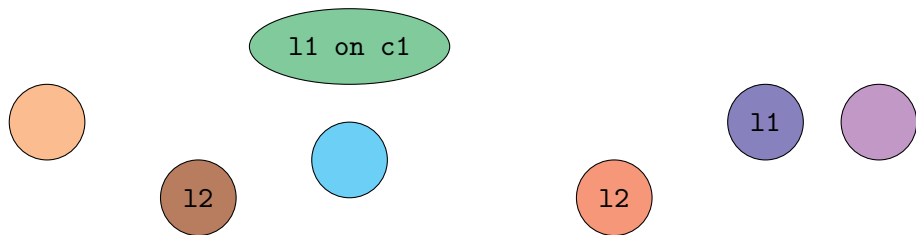
```
node(&mut l1: int, x @ l1) = (z @ l1)
  stack (&mut l2: bool)
  locals (c1 @ l2) (c2 @ l2) (y @ l1 on c1)
  c1 = i(&mut l2)
  c2 = h(&mut l2)
  y = (f on c1)(&mut l1 on c1, x when c1)
  z = (g reset every c1)
      (&l2, &mut l1, c2, merge(c1, y, x whenot c1))
```





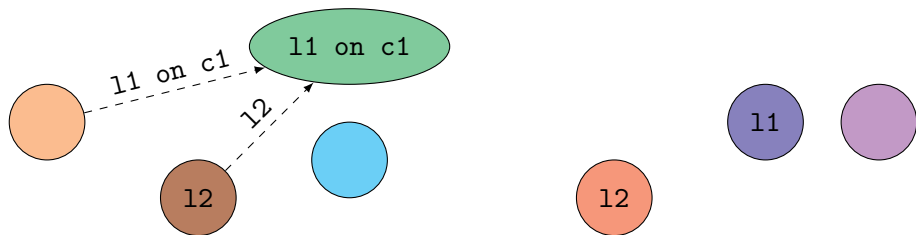
# Scheduling

```
node(&mut l1: int, x @ l1) = (z @ l1)
  stack (&mut l2: bool)
  locals (c1 @ l2) (c2 @ l2) (y @ l1 on c1)
  c1 = i(&mut l2)
  c2 = h(&mut l2)
  y = (f on c1)(&mut l1 on c1, x when c1)
  z = (g reset every c1)
    (&l2, &mut l1, c2, merge(c1, y, x whenot c1))
```



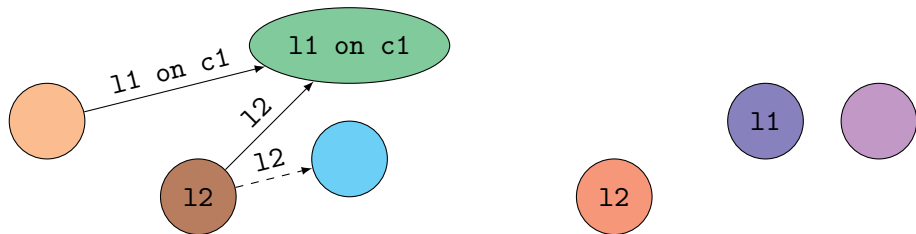
# Scheduling

```
node(&mut l1: int, x @ l1) = (z @ l1)
  stack (&mut l2: bool)
  locals (c1 @ l2) (c2 @ l2) (y @ l1 on c1)
  c1 = i(&mut l2)
  c2 = h(&mut l2)
  y = (f on c1)(&mut l1 on c1, x when c1)
  z = (g reset every c1)
    (&l2, &mut l1, c2, merge(c1, y, x whenot c1))
```



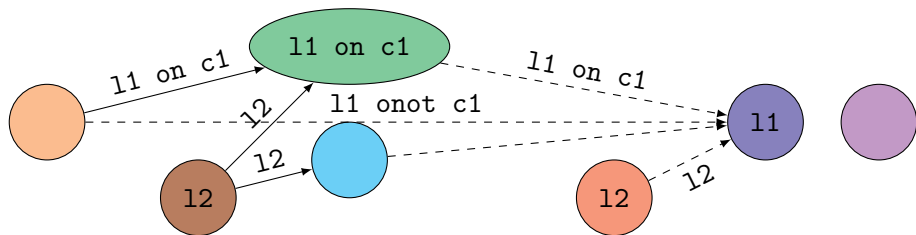
# Scheduling

```
node(&mut l1: int, x @ l1) = (z @ l1)
  stack (&mut l2: bool)
  locals (c1 @ l2) (c2 @ l2) (y @ l1 on c1)
  c1 = i(&mut l2)
  c2 = h(&mut l2)
  y = (f on c1)(&mut l1 on c1, x when c1)
  z = (g reset every c1)
    (&l2, &mut l1, c2, merge(c1, y, x whenot c1))
```



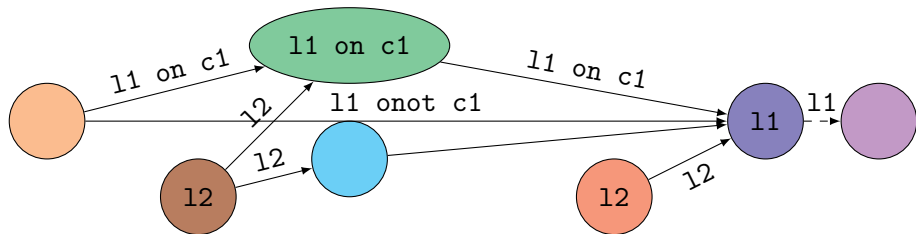
# Scheduling

```
node(&mut l1: int, x @ l1) = (z @ l1)
  stack (&mut l2: bool)
  locals (c1 @ l2) (c2 @ l2) (y @ l1 on c1)
  c1 = i(&mut l2)
  c2 = h(&mut l2)
  y = (f on c1)(&mut l1 on c1, x when c1)
  z = (g reset every c1)
    (&l2, &mut l1, c2, merge(c1, y, x whenot c1))
```



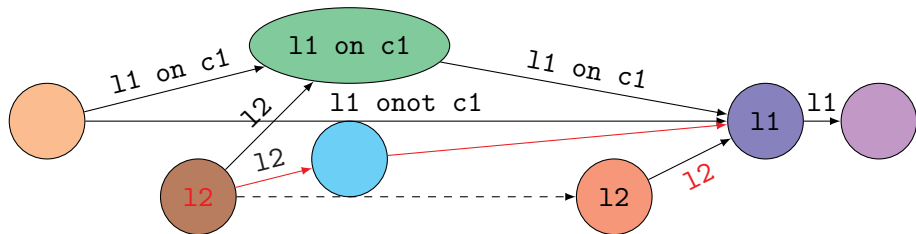
# Scheduling

```
node(&mut l1: int, x @ l1) = (z @ l1)
  stack (&mut l2: bool)
  locals (c1 @ l2) (c2 @ l2) (y @ l1 on c1)
  c1 = i(&mut l2)
  c2 = h(&mut l2)
  y = (f on c1)(&mut l1 on c1, x when c1)
  z = (g reset every c1)
    (&l2, &mut l1, c2, merge(c1, y, x whenot c1))
```



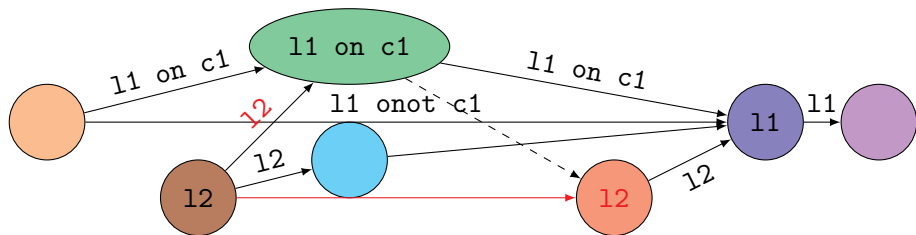
# Scheduling

```
node(&mut l1: int, x @ l1) = (z @ l1)
  stack (&mut l2: bool)
  locals (c1 @ l2) (c2 @ l2) (y @ l1 on c1)
  c1 = i(&mut l2)
  c2 = h(&mut l2)
  y = (f on c1)(&mut l1 on c1, x when c1)
  z = (g reset every c1)
    (&l2, &mut l1, c2, merge(c1, y, x whenot c1))
```



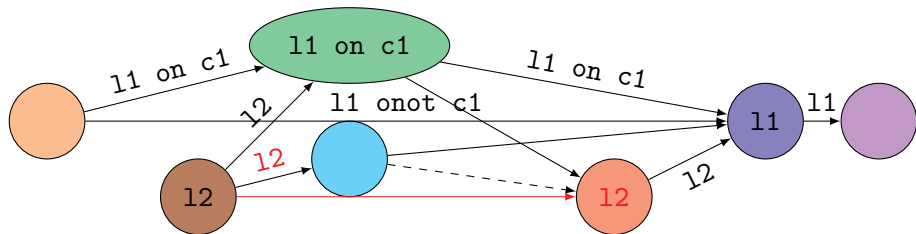
# Scheduling

```
node(&mut l1: int, x @ l1) = (z @ l1)
  stack (&mut l2: bool)
  locals (c1 @ l2) (c2 @ l2) (y @ l1 on c1)
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  y = (f on c1)(&mut l1 on c1, x when c1)
  z = (g reset every c1)
    (&l2, &mut l1, c2, merge(c1, y, x whenot c1))
```



# Scheduling

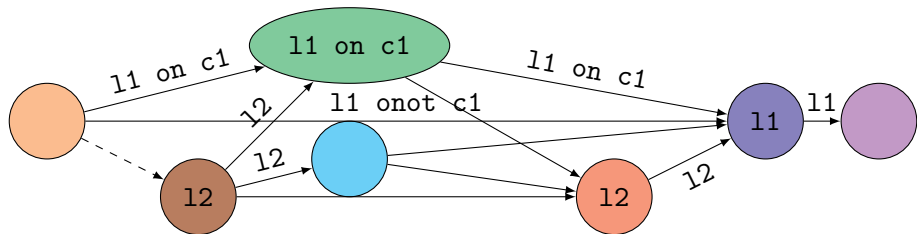
```
node(&mut l1: int, x @ l1) = (z @ l1)
  stack (&mut l2: bool)
  locals (c1 @ l2) (c2 @ l2) (y @ l1 on c1)
  c1 = i(&mut l2)
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  y = (f on c1)(&mut l1 on c1, x when c1)
  z = (g reset every c1)
    (&l2, &mut l1, c2, merge(c1, y, x whenot c1))
```





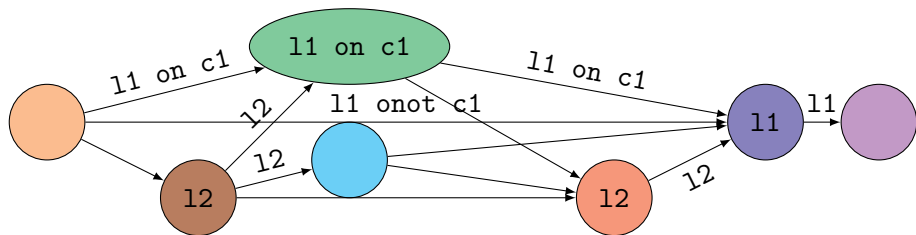
# Scheduling

```
node(&mut l1: int, x @ l1) = (z @ l1)
  stack (&mut l2: bool)
  locals (c1 @ l2) (c2 @ l2) (y @ l1 on c1)
  c1 = i(&mut l2)
  c2 = h(&mut l2)
  y = (f on c1)(&mut l1 on c1, x when c1)
  z = (g reset every c1)
    (&l2, &mut l1, c2, merge(c1, y, x whenot c1))
```



# Scheduling

```
node(&mut l1: int, x @ l1) = (z @ l1)
  stack (&mut l2: bool)
  locals (c1 @ l2) (c2 @ l2) (y @ l1 on c1)
  c1 = i(&mut l2)
  c2 = h(&mut l2)
  y = (f on c1)(&mut l1 on c1, x when c1)
  z = (g reset every c1)
    (&l2, &mut l1, c2, merge(c1, y, x whenot c1))
```



Thank you for your attention!  
Any questions?